

- e) **Matrix operations:** Invert matrix `M` and explain the result. To look for built-in commands, use tab completion and the help system.
- f) **Relational operators:** Assign all elements of `M` greater than 9 the value -1.
- g) **Size:** Get familiar with the `size` command, display the sizes of `a`, `b`, `M`. Make use of the second argument of `size`. Create a matrix of ones in the size of `M`, create a matrix of normally distributed random numbers in the size of `M`.

Exercise 1.3: Plotting in 2D

- a) **Multiple plots:** Define a range of x-values between -4 and 4. Compute sine, cosine, arctangent, and the 3rd order polynomial $y = x + 0.3x^2 - 0.05x^3$ on this interval. Plot the functions into the same window.
- b) **Annotations:** Give the plots different colors, add title, axis labels, and a legend.
- c) **Line styles:** Familiarize yourself with `plot`: line types, plot symbols and predefined colors.

Exercise 1.4: Functions and Scripts, More Plotting

- a) **Functions:** We will now define our first function, `plotcircle` that plots a circle. The function shall take three arguments, the x- and y-coordinates of the circle center and the radius. **Hint:** Create first a range of angles then define vectors of the circle's x- and y-values. Set the property `'Linewidth'` to 4 of the `plot` command.
- b) **Scripts:** Create another file, the script from which we call `plotcircle.m`. We use UpperCamelCase notation for scripts, so call it `PlotCircleDemo.m`. In the script, open a new figure and write an example call of `plotcircle`. Use the command `axis` to adjust the axes and the aspect ratio if needed.
Redefine the function `plotcircle` to take a fourth input argument `color`. The argument should be a 1-by-3 row vector of RGB-values. Extend the `plot` command in `plotcircle` by the `'Color'` property.
Then write a for-loop in the script with 100 randomized radii, positions and RGB-colors and create some post-modern art. Finally, turn the axes off.

Exercise 1.5: Calculate π

We want to calculate π using a Monte Carlo approach. If a circle of radius r is inscribed into a square with side length equal to $2r$, then the area of the circle is πr^2 , while the area of the square is $(2r)^2$. The ratio of the two areas equals $\frac{\pi}{4}$.

If you randomly generate N uniformly distributed points in the square, approximately $N \frac{\pi}{4}$ points fall into the circle. The value of π can then be approximated by $\frac{4 \cdot K}{N}$, with K being the number of points falling into the circle.

- a) **Generate samples:** Generate N points uniformly distributed in the range $[-1, 1] \times [-1, 1]$
- b) **Count inliers:** Determine the number of points K that fall into the unit circle.
- c) **Compute π :** Calculate an estimate for $\hat{\pi}$ and the error $e = |\hat{\pi} - \pi|$.

- d) **Plot:** Plot the circle, plot the square and plot the circle inliers and outliers in two different colors. Give the figure a title that contains the resulting $\hat{\pi}$. Use `plot` to plot the square and familiarize yourself with the `scatter` command for coloring the points. Define an own colormap if needed.

Exercise 1.6: 2D Range Data Segmentation

We want to segment a 2D laser scan using a simple jump-distance criterion. This is useful if we wanted to classify segments, for example, to find people or different objects in such data.

- a) **Get and plot raw data:** Load the laser points from `scan.txt` into a matrix `scan`. The readings are in polar coordinates, angles in the first column, ranges in the second. Put them into row vectors `phi` and `rho`. Convert the points into Cartesian coordinates using `pol2cart`, then plot.
- b) **Preprocess scan:** The scan contains several erroneous readings with a maximum range of 8 meters. This can happen, for instance, when the laser return signal is too weak due to specular reflection or infrared-absorbing surfaces. Filter out all laser points whose ranges are greater than 7.5 meters. Plot the filtered scan.
- c) **Find break points:** Find the break points in the scan. A break point is where the range values of two neighboring points differ (“jump”) by more than 0.3 meters. **Hint:** Use commands `diff` and `find`.
- d) **Build segment data structure:** Build a array of struct for segments with the following fields: a unique identifier, the segment’s begin and end indices, the points of the segments and the segment’s center of gravity.
- e) **Plot segments:** Plot all segments using a different randomized color for each segment. Annotate the segments with their identifier at the respective center of gravity-position using the command `text`.
- f) **Filter segments:** Redo steps 4 and 5 but filter out segments that have less than 3 points.